World Builder's Cookbook

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This document contains equations, constants, and other goodies for world-building calculations. I've found explanations of the principles of world-building, but I often don't find the equations. So here they are. Many of these are lifted from the non-copyrighted version of the sci.space FAQ. Others are taken from Stephen Gillett's excellent book, *World Building*, and the other sources named in the bibliography.

Equations

Acceleration and Distance

Where acceleration is constant, *d* is distance, *v* is velocity, and *t* is time.

Distance	$d = d_0 + vt + \frac{1}{2}at^2$
Velocity	$v = v_0 + at$
Velocity squared	$v_2 = 2ad$
Acceleration on a cylinder of radius r and	$a = 4 \pi^2 r / t^2$
rotation period t:	
Rotation period to give earth "gravity" on a	$t = 2\pi (r/9.8)^{\frac{1}{2}}$
cylinder of radius r	

2	
/	

		Time to travel distance <i>d</i> at acceleration <i>a</i> , given constant acceleration half-way and constant deceleration half-way	$d = \frac{1}{2} at^2$ t = 2 *(d/a) ^{1/2}
Basic Planetary Calculations			
	where	Surface gravity Surface gravity in earth units Escape velocity Orbital velocity Tides (in earth units) (Extremely variable based on undersea geography; this is only a general guideline) Tides (in meters)—see also "Planetary Tides" on page 5 Orbital energy of an object of mass m in an orbit around the sun (mass M) with semimajor axis a	$g = GM/r^{2}$ $g = (d_{P}/d_{E}) \times (\rho_{P}/\rho_{E})$ $v_{esc} = 2\frac{1}{2} \times v_{c} = (2GM/r)^{\frac{1}{2}}$ $v_{orbital} = (GM/a)^{\frac{1}{2}}$ $T = M/R^{3}$ $T = (mR^{4})/(MR^{3})$ $E = -G^{M*m}/(2a)$
		g G M d _P d _E PP PE a R	Acceleration due to gravity Gravitational constant Mass of body Diameter of planet Diameter of earth Density of planet Density of earth Semimajor axis of orbit Planetary radius
Stellar Information		Absolute magnitude from apparent Apparent magnitude from absolute Luminosity from magnitude or, using M for mass Apparent brightness Stellar diameter Size in sky with d & r in same units:	$M = m+5 - 5\log p$ m = M + 5(log ₁₀ p - 1) L = 2.52 ^(4.85 - M) L = M ^{3.5} I = L/R ₂ D = L(T ₂ /t ₂) S = 57.3d/r
	where	(for sizes ~ 20 degrees) Absolute magnitude Apparent magnitude Distance in parsecs Luminosity (in solar units) Intensity (solar constant = 1) Distance of planet (in AU) Distance of planet (any units) Diameter of star (Sol = 1) Diameter of star (any units) Effective temperature of Sol (degrees K) Effective temperature (Sol=1) Effective temperature (star) Size in degrees	M m p L I R r D d T t S

Bolometric corrections

If you're using stars that are somewhat more extreme, you might want to calculate the bolometric magnitude instead. (Bolometric is the total amount of radiation put out by the star.) Add the correction values from this table to the magnitude of the star. For a more complete table showing additional classes, refer to Kaler 1997, p. 263.

Class	Main Sequence	Giants	Supergiants
03	-4.3	-4.2	-4.0
BO	-3.00	-2.9	-2.7
AO	-0.15	-0.24	-0.3
FO	-0.01	0.01	0.14
GO	-0.10	-0.13	-0.1
KO	-0.24	-0.42	-0.38
MO	-1.21	-1.28	-1.3
M8	-4.0		

Table 1: Table of bolometric corrections for some stars. After Kaler 1997, p. 263. If you really need to calculate it, there's an empirical formula and a calculator at <u>http://</u> www.go.ednet.ns.ca/~larry/astro/HR_diag.html.

Schwartzchild Radius

For a black hole of mass M, the Schwartzchild radius r is:

 $r = 2GM/c^2$

Orbits

Period of a Circular Keplerian Orbit

This will hold true for small eccentricities.

$T = 2\pi / (GM/a^3)^{\frac{1}{2}}$	
Gravitational constant	G
Mass of both bodies	М
Radius of orbit	r
Semimajor axis of orbit	а

A pair of planets *cannot* have stable orbits with periods whose ratios are simple fractions (2/1, 3/2, etc) unless they are *very* distant. If they do, they'll be pulling on each other in the *same* direction every time they get close to each other.

Orbital Velocities

Orbital velocities for orbits at a distance r.

а	Semimajor axis
μ	G(m ₁ + m ₂)
r	Distance
$v = [\mu/r]^{\frac{1}{2}}$	Circular orbit
$v = [\mu((2/r) - (1/a))]^{\frac{1}{2}}$	Elliptical orbit
$v = [\mu(2/r)]^{\frac{1}{2}}$	Parabolic orbit
v = [µ((2/r)+(1/a))] ^½	Hyperbolic orbit
$E = -Gm_1m_2/2a$	Energy of object in orbit

Eceentricies

Eccentricities of orbits depending on orbit type, with semimajor axis a and semiminor axis b:

Circular orbit Elliptical orbit Parabolic Hyperbolic orbit	e = 0 e < 1 e = 1 e > 1
The equations are:	
Point of periapsis Point of apoapsis Note:	$R_p = a(1-e)$ $R_a = a(1+e)$ $2a = R_p + R_a$

Eccentricity of orbit	$e = R_p \times V_p 2 / GM$
Eccentricity of orbit	$e = (a^2 + b^2)^{\frac{1}{2}}/a$
Period of orbit	$P_2 = 4\pi^2 / \mu a_3$
	$P = 2\pi/[\mu a_3]^{\frac{1}{2}}$

∆v Between Two Circular Orbits

This is T.N. Edelbaum's equation, normally used for LEO to GEO calculations. Unless there are simplifications I'm not aware of, it should be valid for differences between any two circular orbits around the same primary:

 $\Delta V = (V_1^2 - 2V_1V_2 \cos(\pi/2 \alpha) + V_2^2)^{\frac{1}{2}}$

where

where

V ₁	circular velocity initial orbit
V ₂	circular velocity final orbit
α	plane change in degrees.

Orbit Limits

Roche's Limit

A satellite will break up if its orbit is within Roche's Limit:

L = 2.44 r (density_p/density_s)^{1/3}

Density of planet
Density of satellite
Radius

Titius-Bode Law

GURPS Space uses a variant on this "law" (discovered by Titius, popularized by Bode) for placing planets. Gillett says that current thinking is this is an example of tidal separations in the protocloud; it holds to lesser extents for moon systems as well, but with different parameters.

The classical formula, where r_n is the orbital distance for planet n:

$$r_n = (0.3 \times 2_n) + 0.4 \text{ AU}$$

A more general form, suitable for moons around planets, for planet n:

$$P_n = P_o A^n$$

where:

P _o	Period of orbit of nth planet (traditionally in days)
Po	Period of primary's rotation
А	semimajor axis of the orbit

Minimum Separation and Orbital Stability

There are a lot of factors that determine how closely two planets can orbit without throwing each other out, but a minimum separation is 3.5 times Hill's radius: (This section is particularly fussy and don't bother with it if you don't want to.) This material is my attempt at understanding some stuff that Brian Davis sent me; mistakes are mine, because I'm sure I don't understand it fully yet.

For these equations, the variables are:

а	planet's distance from the star (semimajor axis)
m	planet's mass (or secondary body)
М	star's mass (or primary body)
Fo calculato L	Jill's radius for a particular star /planet pair:

To calculate Hill's radius for a particular star/planet pair:

$$a_hill = a (m / 3M)^{(1/3)}$$

Separation between two bodies should be *at least* three and a half times the larger of the feed limit or the chaos band.

	The feed limit is the same as the Roche limit, 2.4 times the Hill radius. Basically, a planet will "crush and eat" anything orbiting within this radius:					
	Separation_feed > 2.4 a (m / M) ^{$(1/3)$}					
	For smaller planets the chaotic perturbation band is larger than this limit:					
	Sepa	ration_chaos >	1.5 a (m / M) ^(2/7)			
Planetary Insolation	Insolation of a planet determines approximately how much light it gets, and (in solar units) depends on the luminosity of the star and its distance. Brian Davis comments that recent work suggests, conservatively, that I must be between 0.53 and 1.1; see the "fudged temperature" for a more recent measurement.					
	Lumino	on (relative) sity of star e from star	$I = L/D^2$ L D			
	Luminosity is normally done in terms of solar luminosities, so the D is in AUs about luminosity and magnitude.			e		
	Intensit	у	$I = \sigma T^4$			
Rotation and Tidal	Rotation					
Locking	Current thinking is that the rotation period varies tremendously; you can set whatever period you wish. A one extreme is about ninety minutes for earth-like planets; at the other extreme, a satellite may be <i>tide-locked</i> with its primary, always showing the same face (our moon is tide-locked to earth). The minimum time will depend on the density of the body (you don't want it to fly apart). If the satellite orbits in a prograde motion (such as the moon), tidal friction will eventually slow the rotatio of the planet and the satellite will move farther away. If the satellite orbits in a retrograde motion, tidal friction will speed up the rotation of the planet and the satellite will move farther away.					
	Tidal Locking					
	lidal Locking					
	-	anets inside the tidal lock	ing limit will have one face locked towards the star. The	e		
	Very roughly speaking, pla tidal lock limit is in AU:		ing limit will have one face locked towards the star. The 0.0483 (T M^2/ρ) $^{1/6}$	e		
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Planetary Tides	Very roughly speaking, pla tidal lock limit is in AU: Tic where Τ Μ ρ This equation is reflects the for	al Lock limit = ces between two bodies. T nding waves formed by th	0.0483 (T M^2/ρ) ^{1/6} Age of system in years Mass of star in solar masses Density of planet in kg/m ³ The last theory I saw stated that tide heights in specific he shape of the ocean bottom—in other words, highly			
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Planetary Temperatures	Temperature of a blackbody: Albedo Incident light (sun=1) Temp in degrees Kelvin	А І Т			
	$T = 374(1-A)I^{\frac{1}{4}}$				
		sts a fudge factor of about 1.1 for habitable planets:			
	$T = 374 \times 1.1(1-A) I^{\frac{1}{4}}$				
	Intensity of blackbody per unit area:				
	Stefan-Boltzmann constant Temperature, degrees K	σ Τ			
Rocket Equations	Classical rocket equation				
	Where d_v is the change in velocity, I_{sp} is the specific impulse of the engine, v_e is the exhaust velocity, x is the reaction mass, m_1 is the rocket mass excluding reaction mass, g is acceleration due to gravity on earth:				
	Exhaust velocity Change in velocity Or: Ratio of masses	$v_e = g I_{sp}$ $\Delta V = v_e \times ln((m_1 + x)/m_1)$ $(m_1 + x)/m_1) = e^{(d/v)}$			
	Note that (m ₁ +x)/m ₁) is the ratio of the initial mass to the final mass. The exponent d/v is change in velocity over exhaust velocity. For a staged rocket where each stage has the same ratio R of initial to final mass and with <i>n</i> stages, the final delta-vee is:				
	Final Δ	$V = n [v_e ln(R)]$			
	You may notice that's the same as the single stage orbit multiplied by <i>n</i> . Essentially, two stages give you twice the final velocity of a single stage rocket with the same mass ratio, and so on.				
	Relativistic equation				
	For constant acceleration:				
	Time (unaccel.)	$t_u = (c/a) \times \sinh(at/c)$			
	Distance Velocity	$d = (c_2/a) \times (\cosh(at/c)-1)$ $v = c \times \tanh(at/c)$			
Hohmann Transfer Orbits	A Hohman transfer orbit is the minimum energy orbit to get from planet A to planet B, assuming they have circular Keplerian orbits. The orbit is circular, with a tangent at the perihelion of one planet and another tangent at the aphelion of the other. Semimajor axis of planet 1 R ₁				
	Semimajor axis of planet 2	R ₁ R ₂			
	Semimajor axis of the transfer orbit	a=(R ₁ +R ₂)/2			
	Once you have the semimajor axis, you know transfer time: it's <i>half</i> the orbital period for a circular Keplerian orbit of that radius (use equation above). To calculate required ΔV , you need to know the orbital velocity for your transfer orbit at the points where it's tangential to the orbits of the departure and destination planets:				
	$V = (2GM \times [1/r - 1/2a])^{\frac{1}{2}}$				
	The transit time for a Hohmann transfer orbit is half of the orbit, or:				
	$\frac{1}{4} \times P_1 \times (1 + R_2 / R_1)^{3/2}$				
	Ignoring for now the problems of calculating the angle that the destination planet needs to subtend and calculating the launch date; sample calculations for Earth to Mars can be found at: <u>http://www.marsacademy.com/text/angplan.htm</u> <u>http://www.marsacademy.com/text/ladate.htm</u>				
	<u>nttp://www.mars</u>	acauemy.com/text/ladate.ntm			

Constant Acceleration Transit

There's a second kind of easily-calculated, efficient orbit, one that assumes a constant low acceleration (the sort you'd expect from an ion drive or a solar sail).

The acceleration must be very much lower than R/P^2 , where R is the distance from the sun and P is the period of the *outermost* planet. (Note however, that this is *extremely* low; the value of R/P^2 for Earth is 0.015 m/s²; for Mars, it is 0.0065 m/s², or less than 7 ten-thousandths of a G.)

An acceptable approximation of the travel time is:

$$2\pi R_1/(aP_1) \times (1 - R_1/R_2)^{\frac{1}{2}}$$

Where R_1 and P_1 are the distance from the Sun and the period of the inner planet, R_2 the distance between the Sun and the outer planet and a the acceleration of the spacecraft. (Take care to use consistent units: If a is in m/s², P₁ must be in *seconds*.)

You can get a value good enough for story or RPG purposes by doubling $t=(2d/a)^{\frac{1}{2}}$, where *d* is half the distance to the other planet. For example, say that Mars to Earth is (2.279E11 – 1.496E11 meters) 7.83E10 meters, the closest approach. You have a solar sail that gives you 0.001 G acceleration, or 0.01 m/s². The time to accelerate half-way there is:

$(7.83E10/0.01)^{\frac{1}{2}} = (7.83E12)^{\frac{1}{2}} = 2.8E6$ seconds

A little over 32 days. Assume the same time to decelerate, for a total Earth-to-Mars time of about 65 days. A note from the website <u>http://dutlsisa.lr.tudelft.nl/Propulsion/Data/V_increment_requirements.ht</u>m says: "Transfer or trip time for constant thrust spiral is is calculated by dividing total propellant mass by mass flow. Total propellant mass is calculated using the rocket equation also known as Tsiolkowsky's equation. In case of negligible propellant mass (constant acceleration), transfer time can be calculated by dividing the velocity change by the acceleration."

Constants and Values

Some useful constants. Since it's sometimes easier to work things out in solar or terran equivalents, some physical data for our solar system is also included.

For game or story purposes, one or two significant digits is usually all you need, but I've gone to four here.

Constants	G (gravitational constant) c (speed of light in vacuum) Luminosity of sun Solar constant (intensity@1 AU) Planck's constant h "h bar" $h/(2\pi)$ Boltzmann's Constant k Stefann-Boltzman Constant σ Earth gravity acceleration	6.673E-11 Nm ² /kg ₂ 2.998E8 m/s 3.827E26 W 1370 W/m ₂ 6.6262E-34 J-s 1.055E-34 J-s 1.381E-23 J/K 5.670E-8 W/m ₂ /K 9.80665 m/s ₂
Distances	One light year (meters) One parsec (light years)	9.461E15 m 2.063E5 AU 3.262 ly
	Mean earth-moon distance Mean earth-sun distance (1 AU) Mean radius of earth	3.086E16 m 3.844E8 m 1.496E11 m 1.371E6 m
	Equatorial radius of earth Equatorial radius of earth Mean Mercury-sun distance	6.378E6 m 5.79E10 m 0.387 AU
	Mean Venus-sun distance	1.082E11 m 0.723 AU
	Mean Mars-sun distance	2.279E11 m 1.524 AU
	Mean Jupiter-sun distance	7.783E11 m 5.203 AU
	Mean Saturn-sun distance	1.427E12 m

		9.539 AU
	Mean Uranus-sun distance	1.8696E12 m
		19.182 AU
	Mean Neptune-sun distance	4.4966E12 m
		30.058 AU
	Mean Pluto-sun distance	5.9001E12 m
		39.44 AU
Masses	Mass of Sun	1.989E30 kg
	Mass of Earth	5.974E24 kg
	Mass of Moon	7.348E22 kg
	Radius of Earth	6.3E6 m
	Radius of Sun	1.38E9 m
	Average density of Earth	5.5 g/cm ³
		5500 kg/m ³
	Temperature of Sol	5770 K

References

Equations and data were taken from the following references:

World-Building, Stephen L. Gillett, Writer's Digest Books, 1996.

Vehicle Design System, Greg Porter, Blacksburg Tactical Research Center, 1997. "Making Believable Planets," Peter Jekel, Strange Horizons (http://www.strangehorizons.com/2002/ 20020225/planets.shtml)

Some posts in rec.arts.sf.science by Brian Davis (bdavis@pdnt.com) in a thread in December of 2000. The constant acceleration formula came from MA Lloyd in a post to a GURPS mailing list archived at http:// www.rollanet.org/~bennett/gmsf/relspc4.txt.

Bolometric Magnitude from Johnson, H.L.; Morgan, W.W. (1953): Astrophysical Journal, 117: 313.

Bolometric Magnitude reference from Kaler, James B. (1997): Stars and Their Spectra. Cambridge. (Corrected paperback ed.) 300 pp.

Hill radius data from a document by Brian Davis, emailed to me.

Still Under Construction