

Antenas

Análisis de antenas básicas

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Dipolo elemental básico

$$\vec{J} = I \mathbf{d}(x) \mathbf{d}(y) \hat{z} \quad \vec{N} = Il \hat{z}$$

$$\vec{A} = \frac{mI}{4\pi r} e^{-jkr} \hat{z} \quad r \gg l \quad l \gg \lambda$$

$$\vec{E}_{rad} = E_q \hat{q} = -j\omega A_q \hat{q} = j\omega m \frac{Il}{4\pi r} e^{-jkr} \text{sen} q \hat{q}$$

$$\vec{H}_{rad} = H_f \hat{f} = \frac{E_q}{h} \hat{f}$$

$$\bar{\rho} = \text{Re}\{\vec{E} \times \vec{H}^*\} = \hat{r} \frac{(Il)^2}{16\pi^2 r^2} \frac{k\omega m}{r^2} \text{sen}^2 q$$

$$P_r = \iint_S \bar{\rho} d\bar{s} = I^2 P \frac{h}{2} \frac{l^2}{I^2} \frac{4}{3}$$

$$R_r = \frac{P_r}{I^2} = 80 P \frac{l^2}{I^2}$$

$$D = \frac{P_{max}}{P_{rad}/4\pi r^2} = \frac{\bar{\rho}_{max}}{\bar{\rho}_{med}} = \frac{3}{2}$$

$$t = \text{sen}^2 q \Rightarrow \Delta q_{-3dB} = 90^\circ$$

Espira circular elemental

$$\vec{N} = j2\pi a I_1 (k \text{sen} q) \hat{f}$$

$$N_f = jkpa^2 I \text{sen} q, a \ll \lambda$$

$$K = \frac{h}{4I^2} |N_f|^2 = \frac{h}{4I^2} k^2 p^2 a^4 I^2 \text{sen}^2 q$$

$$t(q, f) = \text{sen}^2 q$$

$$P_r = \frac{ph}{6} (ka^4) I^2 \quad R_r = 20p^2 (ka^2) \quad D = \frac{3}{2}$$

$$R_\Omega = \frac{1}{s} \frac{2pa}{2pbd} \quad L = m \ln \left(\frac{8a}{b} \right) - 2$$

$$d_s = \sqrt{p f m s} \quad X_e = L\omega$$

Espira cargada con ferrita

$$V = \oint_C \vec{E} \cdot d\vec{l} = \frac{-d}{dt} \iint_S \vec{B} \cdot d\vec{s} = -j\omega m_e H A$$

$$m_e = \frac{m_f}{1 + D(m_f - 1)} \quad \frac{R_{ferrita} N \text{ vueltas}}{R_{espira}} = N^2 m_e^2$$

Expresiones generales de \vec{N}

Dipolo elemental eléctrico

$$\vec{N} = j\omega \vec{p} \quad \vec{p} = \int_V \mathbf{r}(\vec{r}') \vec{r}' dv'$$

Dipolo elemental magnético

$$\vec{N} = jk \vec{m} \times \hat{r} \quad \vec{m} = \iint_S I \hat{n}' ds'$$

Antenas cilíndricas

$$\vec{J}(\vec{r}') = \hat{z} I(z') \mathbf{d}(x') \mathbf{d}(y')$$

H : altura de un hilo

$$I(z') = I_m \text{sen} k(H - |z'|)$$

$$\vec{N} = \hat{z} 2I_m \frac{\cos(kH \cos q) - \cos kH}{k \text{sen}^2 q}$$

$$D = \frac{\bar{\rho}_{max} 4\pi r^2}{P_r} \quad R_r = \frac{P_r}{I_m^2}$$

Dipolo en $\lambda/2$ (o dipolo de media onda)

$$H = l/4$$

$$\vec{N} = \hat{z} I_m 2 \frac{\cos\left(\frac{p}{2} \cos q\right)}{k \text{sen}^2 q}$$

$$\bar{\rho} = \frac{30 I_m^2}{\pi r^2} \left(\frac{\cos\left(\frac{p}{2} \cos q\right)}{\text{sen} q} \right)^2$$

$$R_r = 73\Omega \quad D = 1.64$$

Dipolo corto

$$H < 0.1\lambda \quad I(z') = I_0 \left(1 - \frac{|z'|}{H} \right)$$

$$P_{rad} = \frac{1}{4} P_{rad_{UNIF}} \Rightarrow R_{rad} = \frac{1}{4} R_{rad_{UNIF}}$$

Uniforme

$$I(z) \quad \text{---} \text{---} \text{---} \text{---} \text{---}$$

$$D=1.5$$

$$t = \text{sen}^2 q$$

$$R = 80p^2 \left(\frac{l}{I} \right)^2$$

Corto

$$I(z) \quad \text{---} \text{---} \text{---} \text{---} \text{---}$$

$$D=1.5$$

$$t = \text{sen}^2 q$$

$$R = \frac{1}{4} R_{uniforme}$$

Monopolos

$$E_M = E_D(z \geq 0)$$

$$I_M = I_D$$

$$P_M = P_D u(z)$$

$$D_M = 2D_D$$

$$P_{rad_M} = \frac{1}{2} P_{rad_D}$$

$$R_{rad_M} = \frac{1}{2} R_{rad_D}$$

$$A_{ef_M} = \frac{1}{2} A_{ef_D}$$

$$l_{ef_M} = \frac{1}{2} l_{ef_D}$$

Teorema reciprocidad

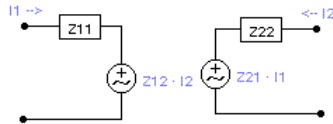
$$\int_V \vec{E}^a \vec{J}^b dv = \int_V \vec{E}^b \vec{J}^a dv$$

$$I_1^a V_1^b (I_1^b = 0) = I_2^b V_2^a (I_2^a = 0)$$

$$V_1 = Z_{11} I_1 + Z_{12} I_2$$

$$V_2 = Z_{21} I_1 + Z_{22} I_2 \Rightarrow Z_{21} = Z_{12}$$

Igualdad impedancias en Tx y Rx



$$Z_1^{Rx} = Z_1^{Tx} \quad Z_1^{Rx} = \frac{V_{ca}}{I_c} = Z_1^{Tx}$$

$$Z_1^{Tx} = \frac{V_1}{I_1} = Z_{11} - \frac{Z_{12} Z_{21}}{Z_{22} + Z_L}$$

Potencia entregada a la carga

$$Z_L = Z_{22}^* \quad V_2 = Z_{22} I_2 + Z_{21} I_1$$

$$P_{R_2} = \left| \frac{Z_{21} I_1}{Z_{22} + Z_{LL}} \right|^2 \text{Re}\{Z_L\} = \frac{|Z_{21}|^2}{4R_{22}} |I_1|^2$$

$$\frac{P_{R_2}}{P_{T_1}} = \frac{|Z_{21}|^2}{4R_{22} R_{11}} = \frac{P_{R_1}}{P_{T_2}}$$

$$\frac{P_{R_2}}{P_{T_1}} = \frac{D_1 A_{ef2}}{4\pi r^2} \quad \frac{P_{R_1}}{P_{T_2}} = \frac{D_2 A_{ef1}}{4\pi r^2}$$

$$\frac{D_1}{A_{ef1}} = \frac{D_2}{A_{ef2}}$$

Igualdad de diagramas

$$I_{CC} = \frac{1}{V} \int_{ant} E_z^i I(z) dz$$

$$V_{ca} = -\frac{1}{I(0)} \int_{ant} E_z^i I_1(z) dz = -E_i I_{ef}$$

Área y longitud efectiva

$$A_{ef} = \frac{P_L}{\wp} = \frac{|V_{ca}|^2}{4R_r \wp} = \frac{|V_{ca}|^2 \mathbf{h}}{|E|^2 4R_r} = \frac{l_{ef}^2 \mathbf{h}}{4R_r}$$

$$l_{ef} = \frac{|V_{ca}|}{|E|}$$

Adaptación

$$P_{L_{max}} = \frac{|V_{ca}|^2}{4R_a} \quad P_L = P_{L_{max}} C_a$$

Coefficiente de desadaptación:

$$C_a = \frac{4R_a R_L}{(R_a + R_L)^2 + (X_a + X_L)^2}$$

$$C_a = 1 \Leftrightarrow Z_L = Z_a^*$$

Ecuación de transmisión

$$\wp = \frac{P_R}{4\pi r^2}$$

$$\wp(\mathbf{q}, \mathbf{f}) = \frac{P_R}{4\pi r^2} D(\mathbf{q}, \mathbf{f}) = \frac{P_e}{4\pi r^2} G(\mathbf{q}, \mathbf{f})$$

$$PIRE = P_{Radiada} D = P_{entregada} G$$

$$P_L = \frac{P_r}{4\pi r^2} D_T A_{efR}$$

Coefficiente de desacoplo de polarización:

$$c_p = |\hat{e}_t \hat{e}_r|^2$$

$$\frac{P_L}{P_r} = \left(\frac{I}{4\pi r} \right)^2 D_T D_R$$

$$G: \text{ganancia} = D \mathbf{h}_{ohmica}$$

$$\mathbf{h}_\Omega = \frac{R_{rad}}{R_{rad} + R_\Omega}$$

Impedancia y autoimpedancias

Cuanto más grueso sea el dipolo, más baja es la resistencia de radiación. Los dipolos gruesos tienen mayor ancho de banda pero una resistencia de radiación pequeña.

Dipolo doblado

$$Z_{DD} = 4Z_D$$

$$D_{DD} = D_D$$