

Model M^0

$A = \{\text{Richard Nixon, John Mitchell, Noam Chomsky, Muhammad Ali}\}$

$F(d) = [[d]]^{M^0} = \text{Richard Nixon}$ $F(j) = [[j]]^{M^0} = \text{John Mitchell}$

$F(n) = [[n]]^{M^0} = \text{Noam Chomsky}$ $F(m) = [[m]]^{M^0} = \text{Muhammad Ali}$

$F(M) = [[M]]^{M^0} = \text{set of people with moustaches} = \{\text{John Mitchell}\}$

$F(B) = [[B]]^{M^0} = \text{set of people who are bald} = \{\text{Richard Nixon, John Mitchell}\}$

$F(K) = [[K]]^{M^0} = \text{set of all pairs of people such that the first knows the second} = \{\langle \text{Richard Nixon, Noam Chomsky} \rangle, \langle \text{Noam Chomsky, Richard Nixon} \rangle, \langle \text{John Mitchell, Richard Nixon} \rangle, \langle \text{Noam Chomsky, Muhammad Ali} \rangle, \langle \text{Richard Nixon, Muhammad Ali} \rangle, \langle \text{Muhammad Ali, Richard Nixon} \rangle\}$

$F(L) = [[L]]^{M^0} = \text{set of all pairs of people such that the first loves the second} = \{\langle \text{Richard Nixon, Noam Chomsky} \rangle, \langle \text{Noam Chomsky, Muhammad Ali} \rangle, \langle \text{Muhammad Ali, John Mitchell} \rangle, \langle \text{John Mitchell, Richard Nixon} \rangle\}$

Model M^1

$A = \{\text{David Crystal, Norah Jones, John Wayne, Mother Teresa}\}$

$F(d) = [[d]]^{M^1} = \text{David Crystal}$ $F(j) = [[j]]^{M^1} = \text{John Wayne}$

$F(n) = [[n]]^{M^1} = \text{Norah Jones}$ $F(m) = [[m]]^{M^1} = \text{Mother Teresa}$

$F(M) = [[M]]^{M^1} = \text{set of people with moustaches} = \{\text{David Crystal, John Wayne}\}$

$F(B) = [[B]]^{M^1} = \text{set of people who are beautiful} = \{\text{Norah Jones, John Wayne}\}$

$F(K) = [[K]]^{M^1} = \text{set of all pairs of people such that the first knows the second} = \{\langle \text{Norah Jones, John Wayne} \rangle, \langle \text{Norah Jones, Mother Teresa} \rangle, \langle \text{John Wayne, Mother Teresa} \rangle, \langle \text{David Crystal, Mother Teresa} \rangle, \langle \text{David Crystal, John Wayne} \rangle\}$

$F(L) = [[L]]^{M^1} = \text{set of all pairs of people such that the first hates the second} = \{\langle \text{David Crystal, Norah Jones} \rangle, \langle \text{John Wayne, David Crystal} \rangle\}$

NOTE: The meaning of logical connectives remain the same across models.

Questions:

(A) Translate the following L_0 wffs into English and compute the missing truth-values, citing semantic rules:

1. $[[M(d)]]^{M^0} = ?$
2. $[[B(d)]]^{M^0} = ?$
3. $[[M(j)]]^{M^0} = ?$
4. $[[B(j)]]^{M^0} = ?$
5. $[[K(m, n)]]^{M^0} = ?$
6. $[[K(n, m)]]^{M^0} = ?$
7. $[[L(n, d)]]^{M^0} = ?$
8. $[[L(j, d)]]^{M^0} = ?$

For example:

(1) Richard Nixon has a moustache. $[[M(d)]]^{M^0} = 1$ iff $[[d]]^{M^0} \in [[M]]^{M^0}$ (by B1). $[[M]]^{M^0} = F(M) = \{\text{John Mitchell}\}$, $[[d]]^{M^0} = F(d) = \text{Richard Nixon}$ (by A). Richard Nixon $\notin \{\text{John Mitchell}\}$. Therefore, $[[M(d)]]^{M^0} = 0$.

(B) Write down all the sentences or wffs of L_0 and their semantic values with respect to model M^1 .

(C) Assuming that unary predicates denote functions in $\{0,1\}^A$ (rather than sets of individuals) and binary predicates denote functions in $(\{0,1\}^A)^A$ (rather than sets of pairs of individuals), write down the semantic values (denotations) of the predicates M, B, K and L in models M^0 and M^1 .

(D) Compute the missing truth-values in (A) assuming – as in (C) – that predicates denote functions rather than sets.