

- 1 Given $A = (4, 3)$ and O is the origin, L is a line through A cutting the positive axes at P and Q .
- Find the equation of L if $\triangle POQ$ has an area of 24.5.
 - Find the equation of the lines L_1 and L_2 , passing through A and at a distance $\sqrt{5}$ units from the origin.
 - If α is the acute angle between the lines L_1 and L_2 . Find the value of α .

- 2 The line L passes through the intersection of
 $59x - 76y + 46 = 0$ and $44x - 27y + 57 = 0$
 If the y-intercept of L is 1, find
- the equation of L .
 - the distance from the origin to L .

- 3
- Find the area of the triangle with vertices $A(-1, 2)$, $B(a - 3, a + 1)$, $C(a, a + 2)$.
 - If these points are collinear, find the values of a .
 - Find the equation of BC .
 - If the line through B and C cuts x- and y-axis at P and Q respectively, find the coordinates of P and Q .
 - If O is the origin, what is the value of a , when area of $\triangle POQ$ is unity.

- 4 The line $L: (1 + \lambda)x + (3 - \lambda)y = 2(1 + 3\lambda)$ passes through a fixed point Q for any value of λ .
- Find the coordinate of Q .
 - If $L \parallel L_1: 2x + 3y = 5$, find the equation of L .
 - If L has x-intercept = 3, find its y-intercept.

- 5 Given two lines $L_1: x - 2y - 4 = 0$
 $L_2: 2x + y - 4 = 0$
 Find a straight line passing through the intersection of L_1 and L_2 and
- with slope 2
 - passing through $(3, -2)$
 - perpendicular to $5x + 3y = 0$.

- 6 A is the point $(1, 3)$
- Find the equation of the straight line with slope m passing through A .
 - Find the slopes of the straight lines which pass through A and are at distances $\sqrt{2}$ units from the point $(2, 6)$.
 - Find the equation of the line through the point $(2, 6)$ cutting the two lines in (b) at points B and C , such that $AB = AC$.
 - Calculate the area of the triangle ABC .

- 7 Two lines L_1 and L_2 pass through $A(1, 1)$ and intersect the line
 $L_3: 3x - y - 12 = 0$
 at the points P and Q respectively. The acute angle between L_1 and L_2 and that between L_2 and L_3 are both θ , where $\tan \theta = \frac{1}{2}$, and L_1 is positively sloped.
- Find, without using tables, the slopes of L_1 and L_2 .
 - Find the equations of L_1 and L_2 .
 - Find the coordinates of P and Q .

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Circle.

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15. Find the equation of the circle such that
 - (a) it passes through the points $A(-2, 2)$, $B(2, 2)$ and $C(-2, -4)$.
 - (b) its centre is at $(-3, 0)$ and it touches the line $x - y - 10 = 0$.
 - (c) it passes through the point $(2, 3)$ and touches the line $2x - 3y - 13 = 0$ at $(2, -3)$.
 - (d) it passes through the points of intersection of the circles $x^2 + y^2 - 2x - 3y - 2 = 0$ and $x^2 + y^2 - 3x + y - 10 = 0$ and the point $P(-2, 1)$.
 - (e) it passes through the points of intersection of the line $x - y + 1 = 0$ and the circle $x^2 + y^2 + 2x - 2y + 1 = 0$, and its centre lies on the line $x + 3y = 3$.
 - (f) Find the equation of the smaller circle whose centre is at the point $(-1, 1)$ and which touches the circle $x^2 + y^2 - 4x - 2y - 11 = 0$.
16. Given the equation $x^2 + y^2 + 2kx - 4ky + 6k^2 - 2 = 0$.
 - (a) Find the range of values of k so that the equation represents a circle with radius greater than 1.
 - (b) Find the locus of the centre of the circle as k varies within the range in (a).
17. The circles $C_1: x^2 + y^2 - 7x + 11 = 0$ and $C_2: x^2 + y^2 - 4x + 6y + 8 = 0$ touches each other externally at P . Find the coordinates of P .
18. Given: $L: y = x$
 $C: (x - 2)^2 + (y - 10)^2 = 18$.
 - (a) Prove that L does not meet the circle C .
 - (b) Find the co-ordinates of the points N and F on the circle C which are respectively the nearest and the furthest from the line L .
19. The circles $C_1: x^2 + y^2 + 4x - 2y + 1 = 0$ and $C_2: x^2 + y^2 + 10x + 4y + 19 = 0$ have a common chord AB .
 - (a) (i) Find the equation of AB .
 - (ii) Find the equation of the circle with AB as a chord such that the area of the circle is a minimum.
 - (b) The circle C_1 and another circle C_3 are concentric. If AB is a tangent to C_3 , find the equation of C_3 .
20. Given the circle $C: x^2 + y^2 + 4x + 2y + 4 = 0$
 - (a) Find the radius and the coordinates of the centre of C .
 - (b) Find the distance from the centre of C to the line $ax + by + c = 0$. Hence, or otherwise, find the equation of the two tangents to C which are parallel to $L: 3x - 4y = 0$.
 - (c) Find the equation of the line passing through the centre of C and perpendicular to the line L . Hence, or otherwise, find the points of contact at which the two tangents obtained in (b) touch C .
21. A circle $C: x^2 + y^2 + 4x - 2y - 11 = 0$ and a straight line $L: x + y = 3$ intersect at A and B . Find the equation of
 - (a) the circle with AB as diameter.
 - (b) the circle which has its centre at $(4, -4)$ and bisects the circumference of C .

22. The line $L: y = mx - 2$ meets the circle $C: x^2 + y^2 = 1$ at the points $A(x_1, y_1)$ and $B(x_2, y_2)$.
 - (a) Show that the length of the chord AB is $2\sqrt{\frac{m^2 - 3}{m^2 + 1}}$.
 - (b) Find the values of m such that
 - (i) L meets C at two distinct points,
 - (ii) L is a tangent to C ,
 - (iii) L does not meet C .
 - (c) For the two tangents in (b) (ii), let the corresponding points of contact be P and Q . Find the equation of PQ .
23. (a) C is a circle with $(0, 1)$ and (p, q) as ends of a diameter. If C cuts the x -axis at two points $(\alpha, 0)$ and $(\beta, 0)$, express $\alpha + \beta$ and $\alpha\beta$ in terms of p and q .
 (b) By drawing a suitable circle, solve the quadratic equation $x^2 + 3x + 1 = 0$.
24. In the figure, A and B are the points $(4, 0)$ and $(8, 0)$ respectively. The equation of C_1 is $x^2 + y^2 - 8x - 2y + 16 = 0$. OH and BH are tangents to C_1 .
 - (a) (i) Show that C_1 touches the x -axis at A .
 - (ii) Find the equation of OH .
 - (iii) Find the equation of BH .
 - (b) In the figure, the equation of OK is $4x + 3y = 0$. The circle $C_2: x^2 + y^2 - 8x + 2fy + c = 0$ is the inscribed circle of $\triangle OBK$ and touches the x -axis at A .
 - (i) Find the values of the constants c and f .
 - (ii) Find area of $\triangle OBH$: area of $\triangle OBK$.
25. Given two circles $(C_1): x^2 + y^2 - 24y = 0$,
 $(C_2): x^2 + y^2 + 24x - 6y + 144 = 0$.

The two external common tangents to the two circles and the line joining their centres meet at the point P .

 - (a) Find the coordinates of the centres and the radii of the two circles.
 - (b) Show that (C_1) and (C_2) touch each other.
 - (c) Show that the x -axis is a common tangent to the two circles.
 - (d) (i) Find the coordinates of the point P .
 - (ii) Find the equation of the other external common tangent to the two circles.
 - (e) Find the equation of the third common tangent to the two circles.

