1996 Paper 2 Question 4

Let
$$f(x) = \begin{cases} x^3 \sin \frac{1}{x} & \text{for } x \neq 0 \\ 0 & \text{for } x = 0 \end{cases}$$

- a. Evaluate f'(x) for $x \neq 0$.
- b. Prove that f'(0) exists.
- c. Is f'(x) continuous at x = 0? Explain.

(6 marks)