# **Spring has Sprung**

**Purpose:** To determine the mathematical relationship between the force applied to a spring and the change in its length for two different springs.

# Hypothesis:

The applied force will be (circle one - directly proportional, inversely proportional, proportional to the square, proportional to the square root) to the change in length ( $\Delta x$ ) of a spring. I think this because:

How will the mathematical model and/or graph of the stiff spring differ from that of the looser spring?

### **Procedure notes:**

You can apply force to the spring by hanging slotted weights from it or by clamping one end to a table and pulling on the spring with a spring scale or Vernier force probe connected to the computer. The Vernier probe will need to be calibrated with a known force or standard weight. The length of the spring can be measured with a ruler. Remember, however, you are graphing the **change** in length so don't forget to record the initial length of the spring. Also, do not stretch the spring out close to its limit – it ruins the spring and complicates the mathematical model.

#### Data:

Length of spring (m)	Change in length, $\Delta x$ (m)	Applied force, F (N)	

# Spring #1 – initial length (m) =

#### Spring #2 – initial length (m) =

Length of spring (m)	Change in length, $\Delta x$ (m)	Applied force, F (N)

#### **Data Analysis/Conclusion:**

Graph force, F (in N) vs change in length of spring,  $\Delta x$  (in m) for both springs on the same graph. Regardless of which was the dependent or independent variable, graph F on the y-axis and  $\Delta x$  on the x-axis. Print out your graphs and attach them to this sheet.

Mathematical models:

Spring #1:

Spring #2:

Was your hypothesis correct? Why or why not?

How do the mathematical models differ for the two springs?

The area under the curve of a force vs displacement graph from gives the elastic potential energy stored in a spring. From your mathematical models above, derive an equation for the elastic potential energy ( $E_{el}$ ) stored in each spring in terms of force (F) and displacement ( $\Delta x$ ) Energy is measured in joules (1 j = 1 Nm = 1 kgm<sup>2</sup>/s<sup>2</sup>).

The accepted equations for force and elastic potential energy for a spring include a term called the spring constant, k (in N/m). What do you think the spring constants are for spring #1 and spring #2? Explain.

### Calibrating the force sensor if you are using a LabPro and a Computer:

- 1. Connect the Force Sensor to CH1 of the LabPro. Make sure your force sensor is set on  $\pm 10$  N (there is a button on the top) for the loose spring and  $\pm 50$  N for the stiffer spring (you may need to recalibrate when you switch to the higher setting).
- 2. Connect the LabPro to the computer and open "Logger Pro 3" on the computer.
- 3. Open Probes and Sensors>Force Sensors>Dual Range Force Sensor> and 10N Dual Range.cmbl or 50N Dual Range.cmbl depending on which spring you are testing..
- 4. Choose Calibrate from the Experiment menu. Select CH1: Dual Range Force. Click on the Calibrate Now button.
- Remove all force from the sensor and hold it vertically with the hook pointed down. Enter a 0 (zero) in the Value 1 field, and after the reading shown for Reading 1 is stable, click இкеер. This defines the zero force condition.
- 7. Click **Done** to complete the calibration of the first Force Sensor.
- You will be using the sensor in a different orientation than that in which it was calibrated. Zero the Force Sensor to account for this. Hold the sensor horizontally with no force applied, and click <u>g Zero</u> and <u>OK</u>.

## Calibrating the force sensor if you are using a LabQuest:

- 1. Connect the Force Sensor to CH1 of the LabQuest. Make sure your force sensor is set on  $\pm 10$  N (there is a button on the top) for the loose spring and  $\pm 50$  N for the stiffer spring (you may need to recalibrate when you switch to the higher setting).
- 2. Choose Calibrate ► CH:1 Force from the Sensors menu.
- 3. Hold the sensor attached to Channel 1 so that you can hang a weight from it but do not attach any weight now.
- 4. Select Calibrate Now.
- 5. Enter 0 as the known value for Reading 1.
- 6. When the voltage reading stabilizes, tap Keep.
- 7. Hang a 1.96 N weight (200 g) from the sensor.
- 8. Enter 1.96 as the known value for Reading 2 and tap Keep when the readings stabilize.
- 9. Select OK.
- 10. You will be using the sensor in a different orientation than that in which it was calibrated. Next you will zero the sensor. To do this
  - a. Hold the sensor with the measurement axis horizontal and no force applied to the hook.
  - b. When the reading stabilizes, choose Zero ► All Sensors from the Sensors menu. The reading for the sensor should be close to zero.