

$$(39) \quad \int_0^{\pi} x \sin 2x dx = \left[-\frac{1}{2} x \cos 2x + \frac{1}{2} \int_0^{\pi} \cos 2x dx \right]_0^{\pi} = \left[-\frac{1}{2} x \cos 2x + \frac{1}{4} \sin 2x \right]_0^{\pi}$$

$$u = x \quad v = -\frac{1}{2} \cos 2x$$

$$du = dx \quad dv = \sin 2x dx$$

$$\frac{1}{2} \int \cos 2x = \frac{1}{4} \sin 2x$$

$$\left[-\frac{1}{2} x \cos 2x + \frac{1}{4} \sin 2x \right]_0^{\pi} = \frac{1}{2} \left[-\pi \cos 2\pi + \frac{1}{2} \sin 2\pi \right] - \frac{1}{2} \left[0 + \frac{1}{2} \sin(0) \right] = \frac{\pi}{2}$$

$$(41) \quad \int_0^1 e^x \sin x dx = \left[\frac{1}{2} e(\sin x - \cos x) \right]_0^1 = \frac{1}{2} [e[\sin 1 - \cos 1] - [-\cos 0]] = \frac{1}{2} [\sin 1 - \cos 1 + 1]$$

Note : use the result of exercise 65 of this section to solve the integral