# The Performance of AICC as an Order Selection Criterion in ARMA Time Series Models

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## **ABSTRAK**

Kajian ini bertujuan untuk menilai prestasi kriteria maklumat Akaike diperbaiki atau AICC (Akaike's Information Corrected Criterion) sebagai kriteria penentuan peringkat dalam pembentukan model Autoregresif Purata Bergerak (Autoregressive Movingaverage) atau ARMA(p,q). Suatu penyelidikan simulasi dijalankan untuk menentukan kebarangkalian di mana kriteria AICC minima telah memilih model *sebenar* dengan tepat. Keputusan yang diperolehi menunjukkan bahawa prestasi kriteria AICC adalah sekadar sederhana. Masalah lebihan pemboleh ubah (over pameterization) wujud, tetapi masalah kurangan pemboleh ubah (under parameterization) berada pada tahap yang minima. Oleh itu, bagi sebarang dua model yang setanding, adalah lebih wajar untuk kita memilih model dengan peringkat p dan q yang lebih rendah.

## **ABSTRACT**

This study is undertaken with the objective of investigating the performance of Akaike's Information Corrected Criterion (AICC) as an order determination criterion for the selection of Autoregressive Moving-average or ARMA (p, q) time series models. A simulation investigation was carried out to determine the probability of the AICC statistic picking up the *true* model. Results obtained showed that the probability of the AICC criterion picking up the correct model was moderately good. The problem of over parameterization existed but under parameterization was found to be minimal. Hence, for any two comparable models, it is always safe to choose the one with lower order of p and q.

Keywords: AICC, ARMA, under/over parameterization

## INTRODUCTION

In the process of time series autoregressive moving-average or ARMA (p, q) modelling, we do not know the *true* order of the model generating the data. In fact it will usually be the case that there is no *true* ARMA (p, q) model, in which case our goal is simply to find one that represents the data optimally in some sense (Brockwell and Davis, 1996). However, the challenge is to decide the optimal orders of p and q (Beveridge and Oickle,

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1994). In a given application, the Box-Jenkins model selection procedure may suggest several specifications, each of which satisfies the diagnostic checks. Some kind of a measure of goodness of fit is therefore needed to distinguish between different models in these circumstances (Harvey, 1993). Many criteria have been suggested for this reason by the past researchers. The Akaike's information corrected criterion (Hurvich and Tsai, 1989) or AICC, among others, is a commonly used criterion. However, its performance must be evaluated. Therefore, the objective of this study is to evaluate the performance of AICC statistics in selecting the *true* ARMA time series model based on a simulation study.

The rest of this paper is organized as follows. The next section discusses the order determination criterion. This is followed by a description of simulation study and a report of simulation results. Finally, the conclusions of the study are presented.

## **ORDER DETERMINATION CRITERIA**

Many criteria have been proposed for the purpose order determination by the past researchers. These include the final prediction error (FPE) criterion, Schwarz-Rissanen criterion (SIC), Bayesian estimation criterion (BEC), Hannan-Qiunn criterion, Akaike's information criterion (AIC) and so on. The latest model selection criterion is the Akaike's information corrected criterion AICC, developed by Hurvich and Tsai in 1989.

There has been considerable literature published on order determination criteria. A brief discussion of these criteria was available in Beveridge and Oickle (1994); de Gooijer et al. (1985), Stoica et al. (1986) and Brockwell and Davis (1996) presented greater theoretical and practical detail and additional references for many of these criteria.

The final prediction error, FPE criterion was original proposed by Akaike (1969, 1970) for AR(p) order determination and was extended to ARMA(p, q) models by Söderström in 1977 (Beveridge and Oickle, 1994). This criterion was established on the basis of minimizing the one-step-ahead mean square forecast error after incorporating the inflating effects of estimated coefficients. The criterion to be minimized is

$$FPE = \hat{\sigma}^2 \frac{n+p+q}{n-p-q} \tag{1}$$

where  $\hat{\sigma}^2$  = variance of white noise,

n = number of observations.

p =order of the autoregressive component,

and q =order of the moving average component.

In 1970, Akaike found that FPE is asymptotically inconsistent and in 1973 he employed information-theoretic considerations to develop the Akaike's information criterion, AIC. This was designed to be an asymptotically unbiased estimate of the Kullback-Leibler index of the fitted model relative to the *true* model (Akaike, 1973). The AIC statistics is defined as

$$AIC = -2 \ln Likelihood (\hat{\phi}, \hat{\theta}, \hat{\sigma}^2) + 2(p+q+1)$$
 (2)

where  $\hat{\phi}$  = a class of autoregressive parameters,

and

 $\hat{\theta}$  = a class of moving average parameters,  $\hat{\sigma}^2$ , n, p and q are as defined in equation (1).

A criterion like AIC that penalizes the likelihood for the number of parameter in the model attempts to choose the most parsimonious model. However, AIC is only asymptotically unbiased and Jones (1975) and Shibata (1976) showed empirical evidences that AIC has the tendency to pick models which are over-parameterized. In view of this, Akaike applied a Bayesian modification to AIC and finally in 1978, he came up with a consistent order selection criterion, known as Bayesian information criterion or BIC; see Akaike (1979). If the data  $\{X_1, ..., X_n\}$  are in fact observations of an ARMA(p, q) process, then Bayesian information criterion is defined to be

BIC = 
$$(n - p - q) \ln \frac{n\hat{\sigma}^2}{n - p - q} + n (1 + \ln \sqrt{2\pi})$$
  
+  $(p + q) \ln \left[ \frac{\sum_{t=1}^{n} X_t^2 - n\hat{\sigma}^2}{p + q} \right]$  (3)

There is evidence to suggest that the BIC is more satisfactory than the AIC as an ARMA model selection criterion since the AIC has a tendency to pick models, which are over-parameterized; see Hannan (1980).

Schwarz (1978) used a Bayesian analysis and Rissanen (1978) applied an optimal data-coding scheme to independently arrive at the same criterion, later known as Schwarz-Rissanen criterion, SIC. The criterion to be minimized is given by

$$SIC = \ln \hat{\sigma}^2 + \left(\frac{p+q}{n}\right) \ln n \tag{4}$$

Geweke and Mease (1981) suggested approximating SIC by Bayesian estimation criterion, BEC.

BEC = 
$$\hat{\sigma}^2 + (p_x + q_x)\hat{\sigma}_x^2 \ln \frac{n}{n - p_x - q_x}$$
 (5)

where *x* denotes a quantity from pre-assigned high order ARMA model that includes all potential models.

Hannan and Quinn (1979) and Hannan (1980) constructed Hannan-Quinn criterion from the law of the iterated logarithm. It provides a penalty function, which decreases as fast as possible for a strongly consistent estimator, as sample size increases. Hannan-Quinn criterion is given by

$$HQ = \ln \hat{\sigma}^2 + 2(p+q) \frac{\ln (\ln n)}{n}$$
 (6)

Hannan and Rissanen (1982) replaced the term  $\ln (\ln n)$  in (6) by  $\ln n$  to speed up the convergence of HQ. This revised version of HQ, however, was found to overestimate the model orders (Kavalieris, 1991).

In 1989, Hurvich and Tsai found that BIC, which was modified from AIC, is not asymptotically efficient. Hence, they suggested a biased corrected version of AIC, known as Akaike's information corrected criterion or AICC. AICC statistics is given by

AICC = 
$$-2 \ln Likelihood (\hat{\phi}, \hat{\theta}, \hat{\sigma}^2) + [2n(p+q+1)]/[n-(p+q)-2]$$
 (7)

where  $\hat{\phi}$  = a class of autoregressive parameters,

 $\hat{\theta}$  = a class of moving average parameters,

 $\hat{\sigma}^2$  = variance of white noise,

n = number of observations,

p =order of the autoregressive component,

q = order of the moving average component,

and *Likelihood* ( $\hat{\phi}$ ,  $\hat{\theta}$ ,  $\hat{\sigma}^2$ ) is the likelihood of the data under the Gaussian ARMA model with parameters ( $\hat{\phi}$ ,  $\hat{\theta}$ ,  $\hat{\sigma}^2$ ).

The penalty factors 2n(p+q+1)/[n-(p+q)-2] and 2(p+q+1), for AICC statistics and AIC statistics respectively, are asymptotically equivalent as  $n \to \infty$ . Moreover, AICC, as AIC or FPE, is asymptotically efficient for autoregressive process. The AICC statistics however, has a more extreme penalty for large order models, which counteract the over fitting nature of the AIC (Brockwell and Davis, 1996). Today, the AICC statistics, as its earlier versions (AIC), has been widely used as one of the order selection criteria in ARMA time series as well as the lag-length selection criteria in econometric modelling processes. Due to its popularity, Brockwell and Davis (1994), for instance, has included the AICC statistics in their computer software package known as "Iterative Time Series Modelling (ITSM)". As the AICC statistics is an important criterion for the selection of order in time series models, its performance must be evaluated. This study hence takes the initiative to explore the probability of minimum AICC criterion in picking up the *true* model based on a simulation study.

## **SIMULATION STUDY**

In this study, a total of 10,000 simulated data series from 10 autoregressive moving average processes were under investigation. These processes were AR(1), AR(2), AR(3), AR(4), MA(1), MA(2), ARMA(1,1), ARMA(1,2), ARMA(2,1) and ARMA(2,2). From there, 100 models were formulated in such a way that each process was assigned a number of 10 models. These models were summarized in the Appendix. For illustration, the 10 models for AR(1) process were those with a parameter  $\phi_1$  value of 0.10, 0.30, 0.50, 0.70, 0.90, -0.30, -0.50, -0.60, -0.80 and -0.95 respectively. Each of these 10 models is in turn replicated into 100 random data series using a different random seed number (less than 10 digits) for each replication. To be consistent in comparison, every random series has 555 observations with a mean value of 111 and a unit variance. No

element of seasonality or trend is involved in this simulated data. The data series are randomly generated using the "Generation of the Simulated Data" option of the *ITSM* software.

The process of time series model fitting in this study involves identification of appropriate models, estimation of parameters and validation of the model. In the process of model fitting, *ITSM* automatically selected a minimum AICC model for each of the data series generated from the AR(1), AR(2), AR(3) and AR(4) processes. As for each of the remaining series, 4 to 9 appropriate models were fitted for model selection purpose. The estimated models are appropriate in the sense that, besides they are stationary and invertible (*ITSM* strictly prohibits the modelling of non-stationary and non-invertible model), they are also required to pass the following formal diagnostic tests of randomness:

- 1. Ljung-Box portmanteau test, which uses the autocorrelations of the residuals to test for the null hypothesis that the residuals are independently and identically distributed (iid);
- 2. McLeod-Li portmanteau test, which tests whether the residuals are from an iid sequence of normally distributed random variables, by using the autocorrelations of the squared-residuals;
- 3. Turning point test, which is a normality test based on the number of turning points;
- 4. Difference sign test, which is used to detect whether a linear trend (implies non-stationary) is present in the residuals;
- 5. Rank test, which is also a stationarity test for the residuals.

These tests are easily checked by "Tests of Randomness of the Residuals" option in the software mentioned earlier. The order of the Yule-Walker model for the residuals is also estimated by this option, to assess whether the residuals of the each estimated model are compatible with the white noise assumption. The informal residuals diagnostic tests, namely plotting the sample autocorrelations function (ACF) and partial autocorrelation function (PACF) are performed by the "Model ACF/PACF" option of *ITSM* software. The details on these diagnostic tests are available in Brockwell and Davis (1996). Out of a class of appropriate models, the order p and q of the minimum AICC model was recorded for each series.

If the estimated p and q of the minimum AICC model matches the simulated model, we say that the AICC criterion has picked up the correct model. If it failed to pick up the correct model, further investigation was carried out to determine whether over parameterization or under parameterization had occurred. Due to the fact that in the computation of AICC statistic the sum of p and q is taken as one term [see equation (7)], the following definitions were proposed. Over parameterization was defined as the sum of the estimated order p and q exceeding sum of the true order p and q, whereas under parameterization happened when sum of the true order p and q exceeding sum of the estimated order p and q. Under these definitions, a minimum AICC model might fail to pick up the correct model, due to neither over parameterization nor under parameterization, however. For instance, ARMA(1,2), ARMA(3,0) and ARMA(0,3) models were clearly different from ARMA(2,1) model, but neither of them was considered over parameterization or under parameterization. This paradox stemmed from

the deficiency in the computation of AICC statistics, which regarded p + q as one term. In this study, these models are treated as mis-specified models.

In this study, for every 100 series of the same model, the probability that the minimum AICC model picks up the correct model, denoted by  $P_c$ , was computed as

$$P_c = \frac{\text{number of time "picks up" occurred}}{100}.$$
 (8)

The probability that the event "over parameterization" happened,  $P_o$ , was calculated as

$$P_o = \frac{\text{number of time "over parameterization" occurred}}{100}.$$
 (9)

Similarly, the probability that the event "under parameterization" happened,  $P_u$ , was given by

$$P_u = \frac{\text{number of time "under parameterization" occurred}}{100}. \tag{10}$$
 Finally, the probability that the event "mis-specification" occured,  $P_m$  was

Finally, the probability that the event "mis-specification" occurred,  $P_m$  was determined by

$$P_m = \frac{\text{number of time "mis - specification" occurred}}{100}.$$
 (11)

## SIMULATION RESULTS

Amongst the 10 models of AR(1) process,  $P_c$  ranged from 0.63 to 0.81 with a mean value of 0.721;  $P_o$  ranged from 0.19 to 0.37 with a mean value of 0.268, while  $P_u$ ranged from 0 to 0.09 with a mean value of 0.011. This means that out of all the 1000 series of AR(1) process, the minimum AICC model matches the correct model 721 of the time; over parameterization occurs 268 of the time and under parameterization happens only 11 of the time. The result for AR(1) process and other the processes in this study was summarized in Table 1. From this table, we could say that AICC statistics is a moderately good model selection criterion, with a probability of picking the true model ranging from 0.366 to 0.795 and a mean value of 0.613. However, chances of over parameterization still exist and in every 100 models, around 17 to 50 models will be over parameterized. As compared to Autoregressive or Moving-average models, over parameterization was found relatively serious in mixed Autoregressive Moving-average models, where the AICC statistics could pick up at most 60 percent of the correct models. The AICC statistics in picking up the "mis-specified" model was negligible in only 4 out of 100 models (not shown). This result suggests that whenever the minimum AICC criterion failed to pick up the *true* model correctly, it was due to over parameterization. This fact that AICC over parameterized could be perceived as supportive to the proponents of parsimonious model such as Box and Jenkins (1976). Hence, for any two comparable models, it is always safe to choose the one with lower order of p and q.

Table 1: Summary of simulation study's results.

No.	Process	Correctly estimated			Over parameterization			Under parameterization		
		Low	High	Mean	Low	High	Mean	Low	High	Mean
1	AR (1)	.63	.81	.721	.19	.37	.268	.00	.09	.011
2	AR (2)	.52	.84	.751	.16	.25	.219	.00	.25	.030
3	AR (3)	.60	.79	.714	.19	.32	.255	.00	.16	.031
4	AR (4)	.25	.78	.631	.15	.33	.233	.00	.60	.097
5	MA (1)	.43	.79	.670	.19	.41	.256	.00	.04	.005
6	MA (2)	.56	.84	.733	.16	.44	.265	.00	.00	.000
7	ARMA(1, 1)	.20	.87	.601	.11	.80	.358	.00	.13	.013
8	ARMA(1, 2)	.45	.74	.594	.26	.55	.406	.00	.00	.000
9	ARMA(2, 1)	.01	.84	.320	.11	.71	.303	.00	.84	.246
10	ARMA (2, 2)	.01	.65	.393	.22	.82	.413	.00	.62	.116
Overall		.366	.795	.613	.174	.500	.298	.000	.273	.055

## **CONCLUSIONS**

The AICC statistics, as its earlier versions (AIC) has been widely used as one of order selection criteria in ARMA time series as well as the lag-length selection criterion in econometric modelling processes. As the AICC statistics is important in ARMA time series modelling and related fields, its performance must be evaluated. This paper evaluates the performance of AICC by determining the probability of the minimum AICC criterion in picking up the *true* model based on a simulation study. A total of 100 models from 10 ARMA processes were used in this study, with 100 replications for each model giving to a total of 10,000 data series. The probability of interest was found to be only 0.613, even though we had use a considerably large sample size. Hence, the performance of AICC in picking up the *true* models is expected to decline in the case of smaller sample size, which usually happens in empirical research. In addition, the minimum AICC criterion, which tries to overcome the over parameterization of the minimum AIC criterion, still has the tendency to overestimate the model orders. This implies that applying AICC criterion in either time series modelling or the selection of lag-length for any lag-length sensitive tests such as unit root and cointegration tests in the related fields would weaken the credibility of the ultimate results.

This study investigates only 10 of the commonly used ARMA(p, q) processes. It could be improved by including more variations of process, especially those with moderately high order, to produce a more influential result. The sample size could also be varied such that the actual performance of the minimum AICC criterion in conjunction with various sample sizes could be uncovered. A computer search algorithm could also be designed to determine a new empirically sound order selection criterion.

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# **Appendix:** List of Simulated Models.

Process	Model	Parameters							
		Φ1	Φ2	Ф3	Ф4	Θ1	Θ2		
	1	0.10	-	-	-	-	-		
	2	0.30	-	-	-	-	-		
	3	0.50	-	-	-	-	-		
	4	0.70	-	-	-	-	-		
AR (1)	5	0.90	-	-	=	-	=		
	6	-0.30	-	-	-	-	-		
	7	-0.50	-	-	-	-	-		
	8	-0.60	-	-	-	-	-		
	9	-0.80	-	-	-	-	-		
	10	-0.95	-	-	-	-	-		
	11	0.70	-0.35	-	_	-	_		
	12	-0.25	-0.85	_	_	-	_		
	13	0.90	-0.20	-	_	-	-		
	14	-0.40	0.40	-	-	-	-		
AR (2)	15	0.20	0.40	-	-	-			
	16	0.20	0.30	-	-	-	-		
	17	0.60	0.30	-	-	-	<u> </u>		
	18	0.40	0.55	-	-	-	-		
	19	0.45	0.35		-	-	-		
	20	-0.50	0.30	-	_	-	-		
	21	0.20	0.20	0.55	-	-			
	22	0.80	0.10	0.09	-	-			
	23	0.10	0.10	0.79	-	-			
	24	0.50	0.05	0.40	_	-	-		
AR (3)	25	0.33	0.33	0.33	_	-	-		
(-)	26	-0.70	0.20	0.50	-	-	-		
	27	0.50	-0.80	0.30	-	-	-		
	28	0.40	0.30	-0.90	-	-			
	29	0.20	0.50		+	-			
	30	0.20	0.30	-0.50 0.10	-	-	-		
	31	0.20	0.30	0.10	0.10	-	-		
	32	0.10	0.10	0.10	0.10	-	-		
	33	-0.10	0.33	-0.10	0.10	+	-		
						-			
AR (4)	34	0.05	0.05	0.20	-0.69	-	-		
(.)	35	-0.60	0.40	0.20	0.05	-	-		
	36	0.21	0.21	0.21	0.21	-	-		
	37	-0.20	-0.10	-0.10	-0.20	-	-		
	38	0.10	0.20	0.30	0.30	-	-		
	39	0.10	0.20	0.05	0.60	-	-		
	40	0.00	0.00	0.00	0.40	-	-		
	41	-	-	-	-	-0.60	-		
	42	-	-	-	-	-0.80	-		
	43	-	-	-	-	0.40	-		
MA (1)	44	-	-	-	-	0.90	-		
IVIA (1)	45	-	-	-	-	0.30	-		
	46	-	-	-	-	0.70	-		
	47	-	-	-	-	0.10	-		
	48	-	-	-	-	0.50	-		
	49	-	-	-	-	-0.20	-		
	50	-	-	-	-	-0.40	-		

# List of Simulated Models (continued).

Process	Model	Parameters							
		Φ1	Φ2	Ф3	Φ4	$\Theta_1$	Θ <sub>2</sub>		
	51	-	-	-	-	0.60	0.40		
	52	-	-	-	-	0.30	0.60		
	53	-	-	-	-	-0.70	0.80		
MA(2)	54	-	-	-	-	0.90	0.30		
	55	-	-	-	-	0.50	-0.70		
	56	-	-	-	-	0.20	0.60		
	57	-	-	-	-	0.40	0.50		
	58	-	-	-	-	-0.60	0.90		
	59	-	-	-	-	0.50	0.50		
	60	-	-	-	-	-0.70	0.50		
	61	0.30	-	-	-	0.90	-		
	62	-0.50	-	-	-	-0.80	-		
	63	0.90	-	-	-	0.30	-		
	64	-0.80	-	-	-	0.50	-		
	65	-0.60	-	-	-	-0.60	-		
ARMA(1, 1)	66	-0.60	-	-	-	0.90	-		
	67	0.40	-	_	_	-0.70	_		
	68	0.80	-	-	-	0.30	-		
	69	-0.60	-	-	-	0.20	_		
	70	0.60	-	-	-	0.80	_		
	71	0.40	-	<del>  -</del>	-	0.60	0.80		
	72	0.80	-	-	-	0.40	0.60		
	73	-0.60	_	_	-	0.30	0.70		
	74	0.50	-	-	_	0.30	0.90		
	75	0.90	-	-	-	0.50	0.60		
ARMA(1, 2)	76	-0.80	-	-	_	0.60	0.35		
	77	0.30	-	-	_	-0.70	0.80		
	78	0.40	-	-	-	-0.60	0.80		
	79	0.70		_	-	0.50	-0.40		
	80	0.20	-	-	-	0.70	0.80		
	81	0.50	0.20	-	-	0.40	-		
	82	0.20	0.50	<del>                                     </del>	-	0.40			
	83	0.90	-0.80	<del>                                     </del>	-	0.80			
	84	0.80	-0.50	-	-	0.60	-		
	85	-0.69	0.26		-	0.90			
ARMA(2, 1)	86	0.10	0.20	-		0.70			
	87	0.10	0.83	-	-	0.70	-		
	88	0.40	0.40	+	-	0.60	-		
	89	0.45	0.15	-	-	0.45			
	90	0.70	-0.70	-	-	-0.70	-		
	91	0.20	0.70	<del>  -</del>	-	0.50	0.50		
	92	0.70	0.70	-	-	0.50	0.50		
	93	0.70	0.20	-	-	0.30	0.30		
	94	0.50	0.45	-	-	0.70	0.70		
	95	0.30	0.45	-	-	0.80	0.20		
ARMA(2, 2)	96	0.70	-0.80	-	-	0.50	0.13		
,	97	0.60	0.35	-	-	-0.90	0.40		
	98								
		-0.70	0.25	-	-	0.30	0.80		
	99	-0.35	0.60	-	-	1.10	0.90		
	100	0.60	-0.40	-	-	0.30	0.30		